

The FORSYDEsystem which performs the the Fast Fourier Transform can be defined in terms of atoms as:

$$\mathbf{fft}_S k vs = \mathbf{bitrev}_S((\mathit{stage} \diamond \mathit{kern}) \diamond vs) \quad (1)$$

where the constructors

$$\mathit{stage} wdt = \mathbf{concat}_S \circ (\mathit{segment} \diamond \mathit{twiddles}) \circ \mathbf{group}_S wdt \quad (2)$$

$$\mathit{segment} t = \mathbf{undual}_S \circ (\mathit{butterfly} t \diamond) \circ \mathbf{dual}_S \quad (3)$$

$$\mathit{butterfly} w = ((\lambda x_0 x_1 \rightarrow x_0 + wx_1, x_0 - wx_1) \triangle) \oplus \quad (4)$$

are aided by the number generators

$$\mathit{kern} = \mathbf{iterate}_S (\times 2) 2 \quad (5)$$

$$\mathit{twiddles} = (\mathbf{reverse}_S \circ \mathbf{bitrev}_S \circ \mathbf{take}_S (\mathbf{lgth}_S vs/2))(\mathit{wgen} \diamond \langle 1.. \rangle) \quad (6)$$

$$\mathit{wgen} x = - \frac{2\pi(x-1)}{\mathbf{lgth}_S vs} \quad (7)$$